Homework #1 (100 points) - Show all work on the following problems:

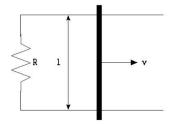
(Grading rubric: Solid attempt = 50% credit, Correct approach but errors = 75% credit, Correct original solution = 100% credit, Copy of online solutions = 0% credit)

Problem 1 (20 points): Consider two concentric metal spherical shells, of radius a and b (a < b), separated by conductive material with conductivity σ .

1a (10 points). If the two shells are maintained at a potential difference ΔV , what current I flows from one to the other?

1b (**10 points**). What is the effective resistance *R* of this configuration?

Problem 2 (30 points): Consider a metal bar of mass m, sliding frictionlessly on two parallel conducting rails a distance l apart, with a resistor R connected across the rails. A uniform magnetic field B points into the page and fills the entire region.



2a (10 points): If the bar moves to the right with speed *v*, what is the current (magnitude and direction) in the resistor?

2b (10 points): What is the magnetic force (magnitude and direction) on the bar?

2c (10 points): If the bar starts out with speed v_0 at t = 0, what is its speed at a later time t?

Problem 3 (10 points): To compute the magnetic flux $\Phi_B = \int \vec{B} \cdot \vec{da}$, which is differentiated to determine the motional EMF around a loop, we do not need to specify the surface over which the flux should be calculated, only the loop that forms the boundary of that surface. Why doesn't the specific surface matter?

Problem 4 (20 pointss): Consider a square loop of wire with sides of length a, lying in the x-y plane, extending from the origin to the point (x,y) = (a,a). If the magnetic field is $\vec{B}(x,y,t) = ky^3t^2\hat{z}$ (with k a constant), what is the EMF induced around the loop?

Problem 5 (20 points): Consider a long solenoid of radius a, with n turns per length, with a current that increases linearly with time (i.e. $I_s(t) = kt$, with k a constant). If a loop of wire with resistance R is placed around the solenoid, what current I_r flows in the loop? Is the loop current in the same direction or the opposite direction as the solenoid current?

